

Module-II (SAT)

Sensing Elements

1. Resistive sensing element

- Potentiometer
- Thermistor
- Helipot
- Resistance Thermometer or, RTD (RTD- Resistance temp. Detector)
- Strain Gauge

It can sense temperature, strain, displacement, heat, loss etc.

$$R = \rho \frac{L}{A}$$

Potentiometer [POT]

Passive transducer: Those transducer which requires external power for energy conversion is known as passive transducer.

Active transducer: Those transducer which don't require external power sources for energy conversion, known as active transducer.

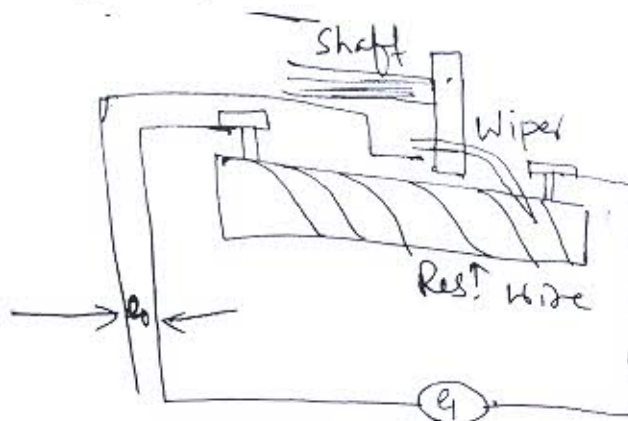
Ex: - Piezo-electric Crystal, Thermocouple

Potentiometer is used for displacement measurement.

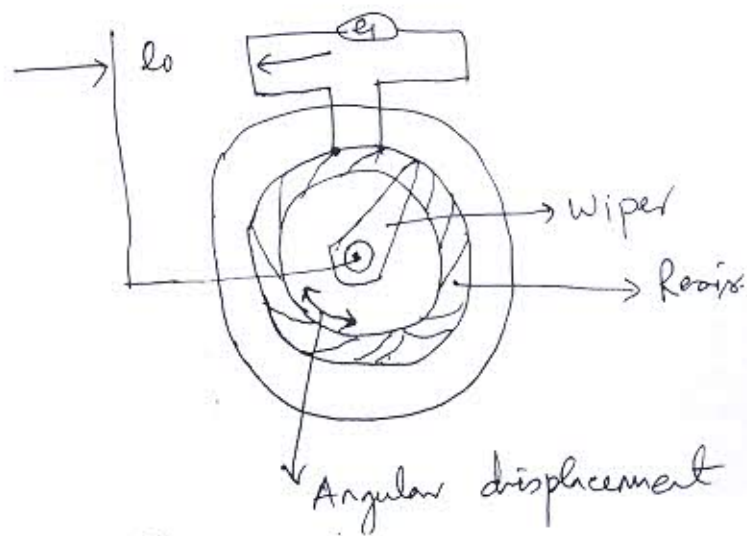
- Strain → Strain Gauge
- Temperature → Thermistors

It is a potential divider called POT and it is a passive sensing element.

It measures linear as well as angular displacement.

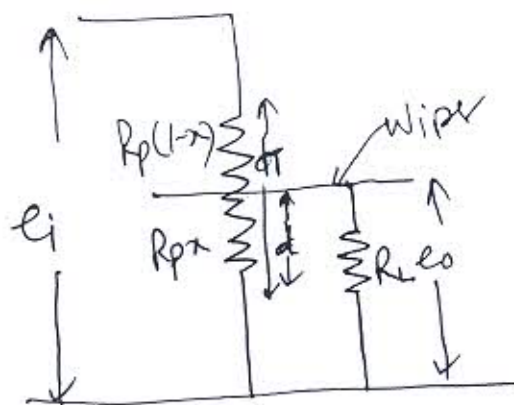


(1) Translational POT



(2) Rotational POT

Schematic Diagram:



$d \rightarrow$ length covered by the wiper

$dT \rightarrow$ Total length of the resistive element

$R_p \rightarrow$ Total Resistance of the POT

$d/dT = x =$ Fractional Displacement

$$E_{th} = \frac{e_i \times R_p x}{R_p}$$

$$E_{th} = e_i \cdot x$$

$$R_{Th} = R_p(1-x) \parallel R_p x = \frac{R_p(1-x) \cdot R_p x}{R_p} = R_p \cdot x \cdot (1-x)$$

$$V_L = \frac{E_{th} R_L}{R_{th} + R_L} = \frac{e_i x R_L}{R_p x(1-x) + R_L}$$

$$V_L = \frac{e_i x R_L}{R_p x(1-x) + R_L} \rightarrow \text{Non - Linear Equation}$$

when R_L is large linearity can be obtained

$$V_L = \frac{e_i x R_L}{R_L \left[\frac{R_p}{R_L} x(1-x) + R_L \right]} \Rightarrow V_L = \frac{e_i x}{\frac{R_p}{R_L} x(1-x) + 1}$$

When $R_L = \infty$

$$V_L = e_i x \rightarrow \text{Linear property of potentiometer}$$

→ POT are of two types: -

- i) *Wire Wound type*: - In this type 0.01 mm diameter of platinum or nickel alloy each wound over an insulated former.
- ii) *Plastic thin film type*: - These have zero resolution but have higher temperature co-efficient of resistance. This covers displacement span from 25-250mm with Non-linearity up to $\pm 0.04\%$ and resistance value from 500 ohm- 80 K ohm.

Resistance Thermometer (RTD)

It is made up of metal like Nickel, Cr and Pt.

→ Platinum (Pt) is suitable metal for construction of RTD's because it is chemically inert and the range of temperature it can withstand is very large.

→ Characteristics of Pt. with respect to temperature is linear. General relationship between change in resistance and change in temperature of any metal is given by

$$R_T = R_0 [1 + \alpha T + \beta T^2 + \gamma T^3 + \dots]$$

R_T = Resistance at T °C

R_0 = Resistance at 0 °C

α, β, γ = Temperature co-efficient of resistance of the metal

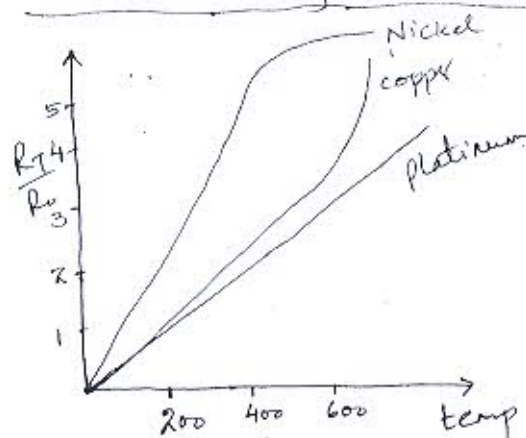
→ β, γ are Non-linear terms and values are very small.

$$R_T = R_0 [1 + \alpha T]$$

→ A typical Platinum element has $R_0 = 100$ ohm and $R_{100} = 138.5$ ohm

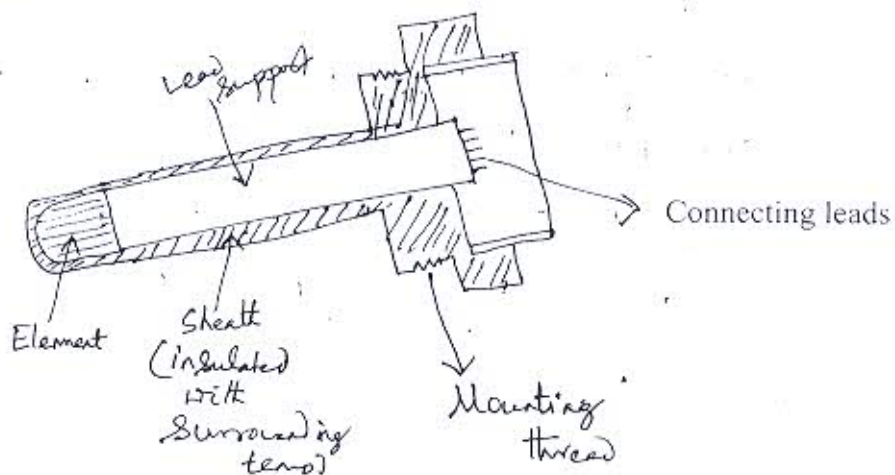
→ $[R_{100} - R_0]$ = Fundamental Interval

characteristics of metal with temp



Requirement of Conductivity material to be used in RTD:

- 1) A change in resistance of material for unit change in temp should be as large as possible (sensitivity is High)
- 2) Resistance of material should have continuous and stable relationship with temperature.

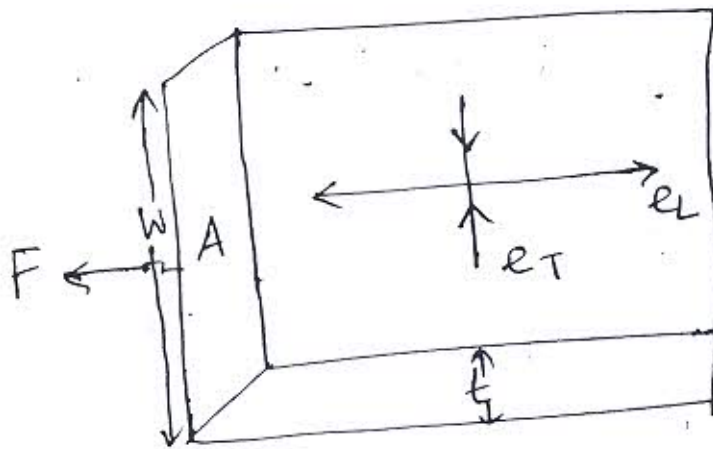


Thermistor (Thermal Resistor)

→ These are resistive sensing element made up of semiconductor material used for measurement of temperature.

→ The material used are metallic oxide of Cu, Ni, Fe, Co, Cr, Mn etc.

Derivation of Gauge Factor:



$$R = \rho \frac{L}{A}$$

$$\Delta R = \left(\frac{\partial R}{\partial L} \right) \Delta L + \left(\frac{\partial R}{\partial A} \right) \Delta A + \left(\frac{\partial R}{\partial \rho} \right) \Delta \rho$$

$$= \frac{\rho}{A} \Delta L + \frac{\rho L}{-A^2} \Delta A + \frac{L}{A} \Delta \rho$$

$$A = w \times t$$

$$\Delta A = \frac{\partial A}{\partial w} \Delta w + \frac{\partial A}{\partial t} \Delta t$$

$$= t \cdot \Delta w + w \cdot \Delta t$$

$$\frac{\Delta A}{A} = \frac{\Delta w}{w} + \frac{\Delta t}{t} = e_T + e_T$$

$$\Rightarrow \frac{\Delta A}{A} = 2e_T$$

$$\Delta R = \rho \frac{\Delta L}{A} - \frac{\rho L}{A} 2e_T + \frac{L}{A} \Delta \rho$$

$$\frac{\Delta R}{R} = \frac{\Delta L}{A} - 2e_T + \frac{\Delta \rho}{\rho}$$

$$\frac{\Delta R}{R} = e_L - 2(-ve_L) + \frac{\Delta \rho}{\rho} = e_L + 2ve_L + \frac{\Delta \rho}{\rho}$$

$$\Rightarrow \frac{\Delta R}{R} / e_L = 1 + 2\nu + \frac{\Delta \rho}{e_L \rho}$$

Gauge Factor is the change in unit resistance per strain

$$GF = \frac{\Delta R / R}{e} = \frac{\Delta R / R}{\Delta L / L}$$

$$GF = 1 + 2\nu + \frac{1}{e_L} \frac{\Delta \rho}{\rho}$$

Due to change
in length

Due to change
in Area

Due to change in Piezo-resistive
effect (very small)

Only for semiconductor gauge we
have to consider this effect

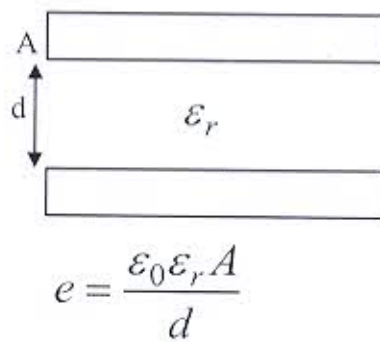
→ For most of the metals Poisson ratio is approximately equals to 0.3 and the Piezo-resistive effect is 0.4.

→ So, metal gauge factor is around 2.

→ For semiconductor strain gauge Piezo-resistive effect term is very large. So gauge factor (GF) of Semiconductor strain gauge is very large. Hence Sensitivity is high for semiconductor type strain gauge.

→ Disadvantages of semiconductor strain gauge is its resistance decreases with increase in temperature and consequently there is a decrease in gauge factor of strain gauge i.e. decrease in sensitivity.

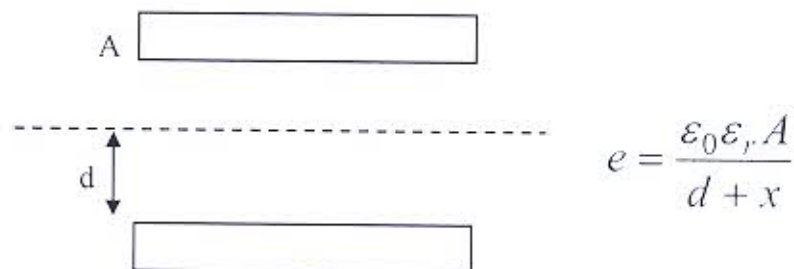
2. Capacitive Sensing Elements



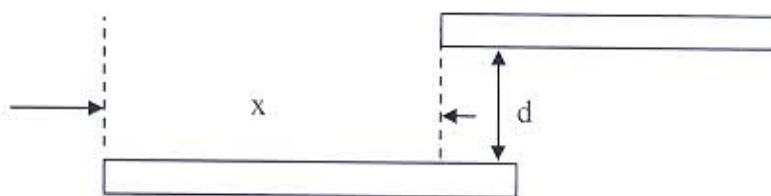
ϵ_0 = Permittivity of free space ($8.85 \times 10^{-12} \text{ F/m}$)

ϵ_r = Permittivity of relative medium

a) Variable displacement Sensor



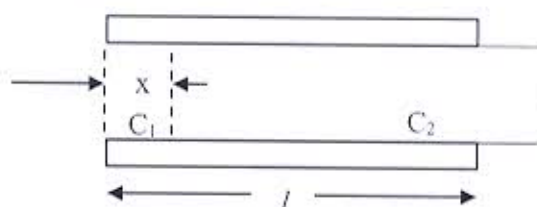
b) Variable Area Sensor



W = width of the plate

$$e = \frac{\epsilon_0 \epsilon_r (A - wx)}{d}$$

c) Variable Di-electric type sensor

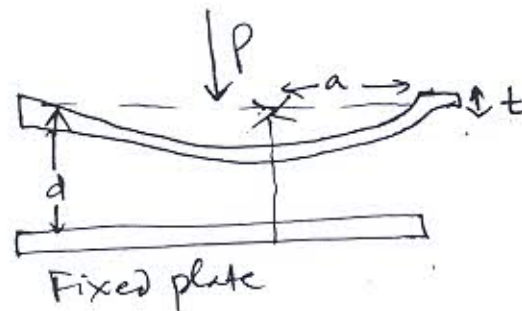


$$C = C_1 + C_2$$

$$C = \frac{\epsilon_0 \epsilon_{r1} wx}{d} + \frac{\epsilon_0 \epsilon_{r2} w(l-x)}{d}$$

$$\Rightarrow C = \frac{\epsilon_0 w}{d} [\epsilon_{r2} l - x(\epsilon_{r2} - \epsilon_{r1})]$$

d) Capacitive Pressure Sensor



$$y = \frac{3}{16} \cdot \frac{(1-\nu^2)}{Et^3} (a^2 - r^2) \rho$$

$$\frac{\Delta C}{C} = \frac{(1-\nu^2)a^4}{16Edt^3}$$

Where, $P \rightarrow$ Applied Pressure

$\Delta C \rightarrow$ Change in Capacitance

$a \rightarrow$ Radius of the Diaphragm

$r \rightarrow$ Radius in which we are applying pressure to generate displacement

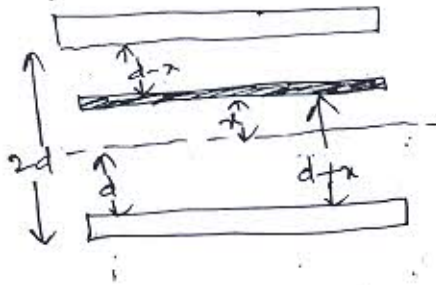
$t \rightarrow$ Thickness of Diaphragm

$E \rightarrow$ Young's modulus of Material

$\nu \rightarrow$ Poisson's Ratio

$C \rightarrow$ Original Capacitance of capacitor before application of pressure

e) Three Plate Differential or, Push Pull Displacement Sensor

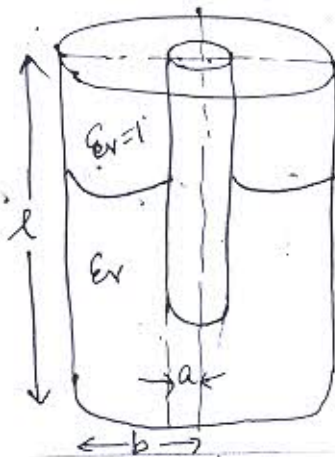


$$C_1 = \frac{\epsilon_0 \epsilon_r A}{d - x}$$

$$C_2 = \frac{\epsilon_0 \epsilon_r A}{d + x}$$

For avoiding non-linearity we have to incorporate this with a bridge circuit.

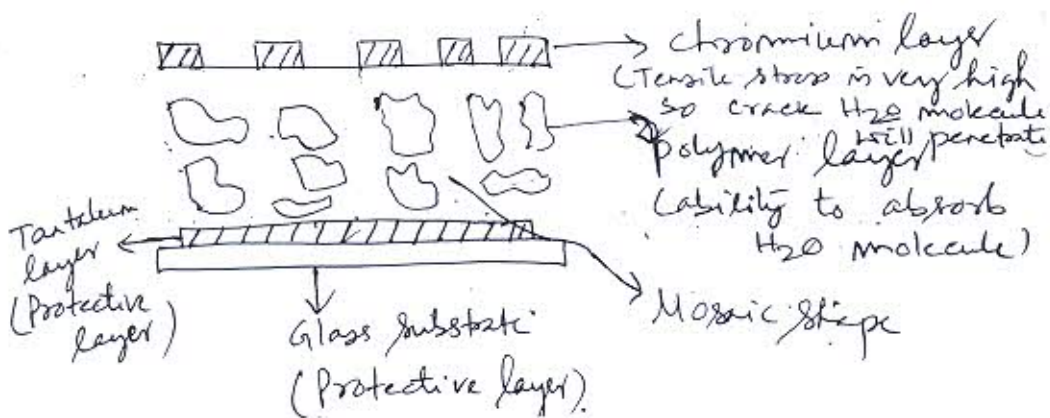
f) Capacitive level Sensor



$$\text{Capacitance / length} = \frac{2\pi\epsilon_0\epsilon_r}{\log_e(b/a)}$$

$$C = \frac{2\pi\epsilon_0\epsilon_r h}{\log_e(b/a)} + \frac{2\pi\epsilon_0\epsilon_r (l-h)}{\log_e(b/a)}$$

g) Thin Film Capacitance Humidity Sensor



→ If all the H_2O molecule is not going to be absorbed by the polymer layer, then it won't go down.

$$\Delta C \propto \text{Relative Humidity}$$

$$C = (375 + 1.7 \text{ RH}) \text{ pF}$$

RH \rightarrow Relative Humidity

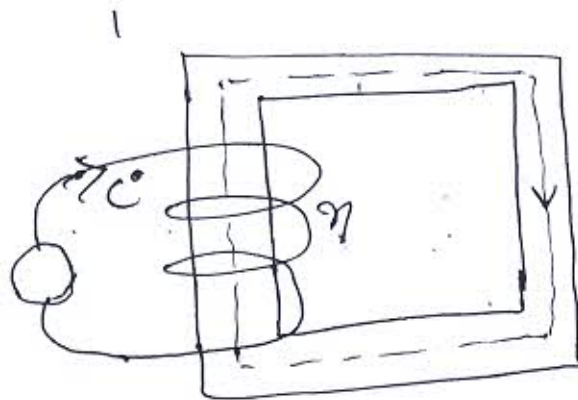
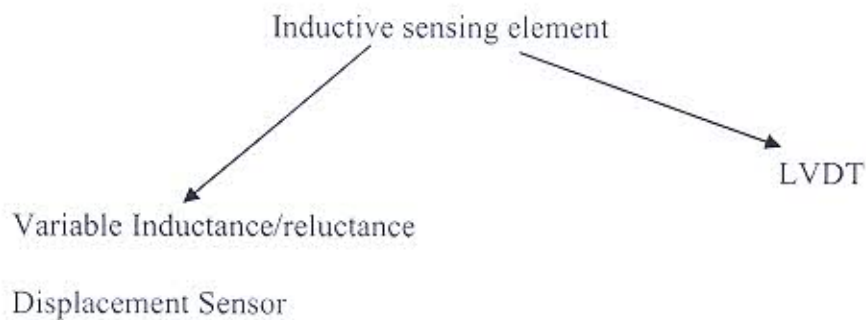
pF \rightarrow Pico Farad

\rightarrow The humidity sensor has an input range of 0 to 100% RH and a capacitance of 370 pico-Farad which RH is 0% and a linear humidity of 1.7 pF per percent RH.

\rightarrow The di-electric medium is characterised by a word called **loss tangent**.

$$\tan \delta = \frac{1}{\omega CR}, Q = R \sqrt{\frac{L}{C}}$$

3. Inductive Sensing Element



$$mmf = \phi \times R \quad (R \rightarrow \text{Reluctance})$$

$$\phi = \frac{ni}{R}, \quad N = \frac{n^2 i}{R}$$

$$L = \frac{n^2 i}{R_i} = \frac{n^2}{R}, \text{ Inductance(L)} = \frac{\text{Total flux}}{\text{Current}}$$

$$R = \frac{l}{\mu \mu_0 A}$$

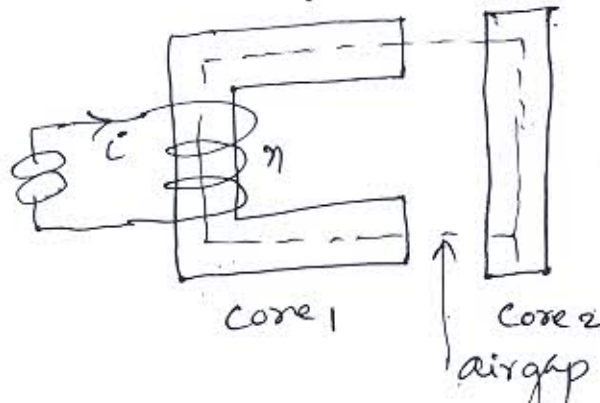
Where, l = Total length of flux path

A = Cross-sectional area of flux path

μ_0 = Permeability of Free space

$$\mu_0 = 4\pi \times 10^{-7} \text{ Henry/m}$$

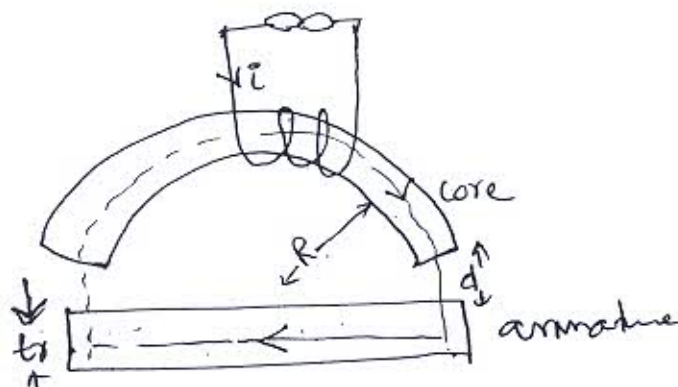
μ = Relative Permeability



$$R_{\text{total}} = R_{\text{core1}} + R_{\text{air gap}} + R_{\text{core2}}$$

Variable inductance/reluctance displacement Sensor

- Variable reluctance displacement Sensor
- Push pull or, Differential displacement sensor



$$R_{total} = R_{core} + R_{air\ gap} + R_{armature}$$

$$R_{core} = \frac{\pi R}{\mu_0 \mu_c \pi r^2} = \frac{R}{\mu_0 \mu_c r^2}$$

$$R_{air\ gap} = \frac{2d}{\mu_0 \pi r^2}$$

$$R_{armature} = \frac{2R}{\mu_0 \mu_A 2rt_r} = \frac{R}{\mu_0 \mu_A rt_r}$$

$$\begin{aligned} R_{total} &= \frac{R}{\mu_0 \mu_c r^2} + \frac{2d}{\mu_0 \pi r^2} + \frac{R}{\mu_0 \mu_A rt_r} \\ &= \frac{R}{\mu_0 r} \left[\frac{1}{\mu_c r} + \frac{1}{\mu_A t_r} \right] + \frac{2d}{\mu_0 \pi r^2} \end{aligned}$$

$$R_T = R_0 + kd$$

$$\Rightarrow R_0 = \frac{R}{\mu_0 r} \left[\frac{1}{\mu_c r} + \frac{1}{\mu_A t_r} \right]$$

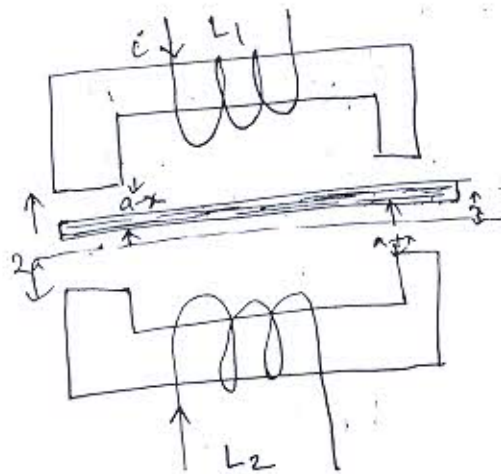
$$k = \frac{2}{\mu_0 \pi r^2} \quad [\text{k value depends upon the structure of the material}]$$

$$L_T = \frac{n^2}{R_T} = \frac{n^2}{R_0 + k.d} = \frac{\frac{n^2}{R_0}}{\frac{R_0}{R_0} + \frac{k.d}{R_0}} = \frac{L_0}{1 + \alpha d}$$

$$\left[\therefore L_0 = \frac{n^2}{R_0} \text{ and } \alpha = \frac{k}{R_0} \right]$$

$L_0 \rightarrow$ Inductance of sensor at zero air gap, k & α depends upon the structure of the sensor.

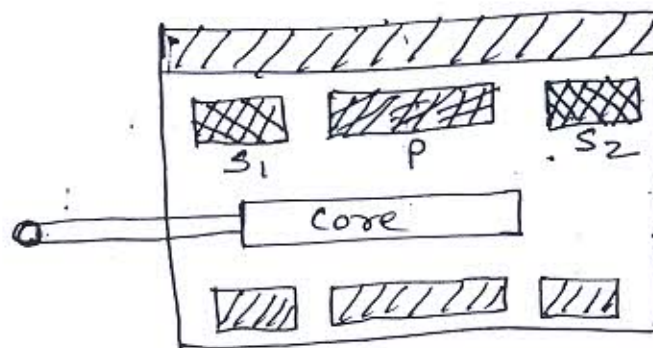
Push pull or, Differential displacement sensor



$$L_1 = \frac{L_0}{1 + \alpha(a-x)}, \quad L_2 = \frac{L_0}{1 + \alpha(a+x)}$$

→ In order to avoid non-linearity, we design this type of sensor. We have to incorporate this with bridge circuit.

LVDT (Linear Variable Differential Transformer)



→ The soft iron core makes a flux linkage between the primary winding and the two secondary winding.

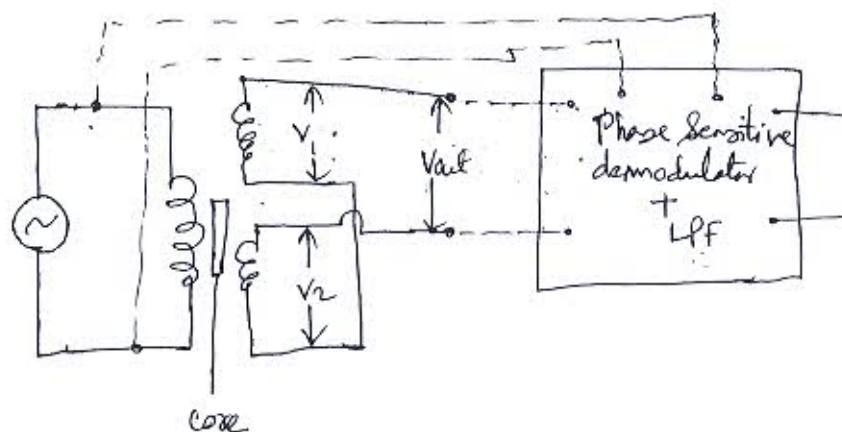
→ The two secondary windings are identically placed either side of the primary windings.

→ Number of turns of two secondary windings are equal.

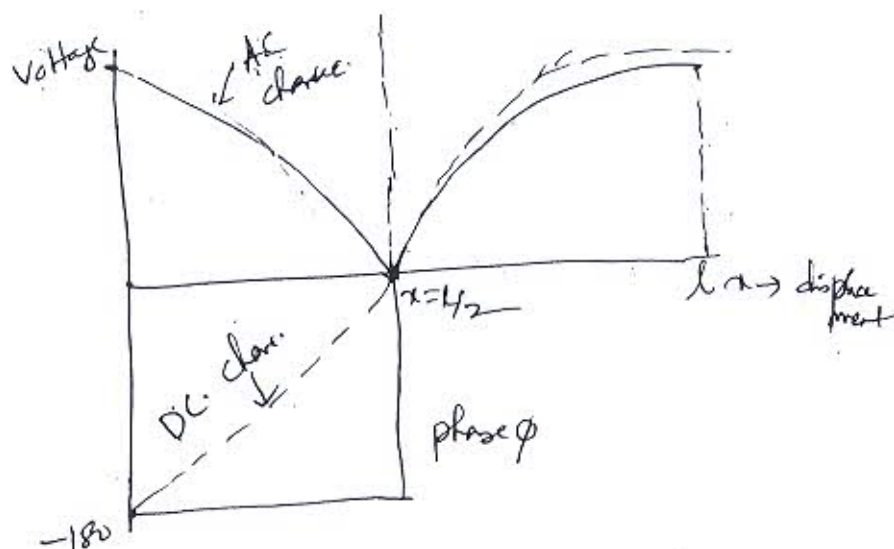
→ The core is made up of high permeability (unwanted fizzer component) Nickel iron which is having low harmonics, low null voltages and is of high sensitivity.

→ The core is slotted longitudinally to reduce the eddy current loss. (Current due to the back e.m.f.)

LVDT Electrical equivalent Circuit:



→ The two secondary coils are connected in series so as to get one output.



→ Phase sensitive demodulator- to produce positive voltage and negative voltage.

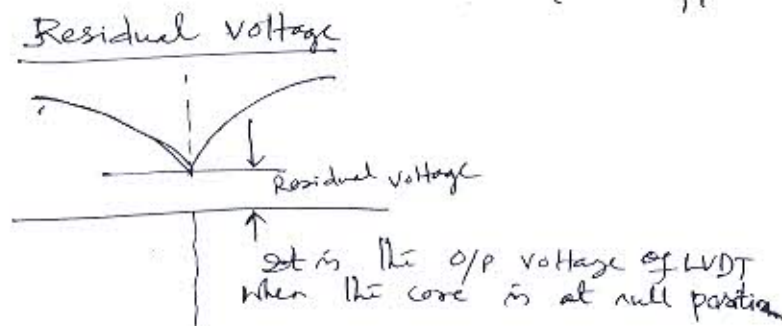
Note

Low Pass Filter (LPF)

→ The Band width B.W. of LPF is less than the sampling frequency to filter out the carrier signal and more than maximum frequency not to filter out the measurement signal.

→ Frequency of AC applied to primary winding is in the range of 50Hz-20KHz. The Primary winding is excited by AC source produce an alternating magnetic field which includes A.C voltage in the two secondary winding.

→ To represent the output from the two secondary's in to a single voltage, the two secondaries are connected in series opposition.



Reason for Occurrence of Residual Voltage in LVDT

- This may be due to an account of presence of harmonics in the input supply voltage and also the harmonics present or produced in the output voltage.
- The Residual voltage may be due to either an incomplete magnetic or, electrical unbalance.

4. Electromagnetic Sensing Element

→ Eg: - Velocity Sensor

Variable Reluctance Tacho generator for measurement of angular velocity

→ These sensors are based on Faraday's laws for measurement of linear and angular velocity.

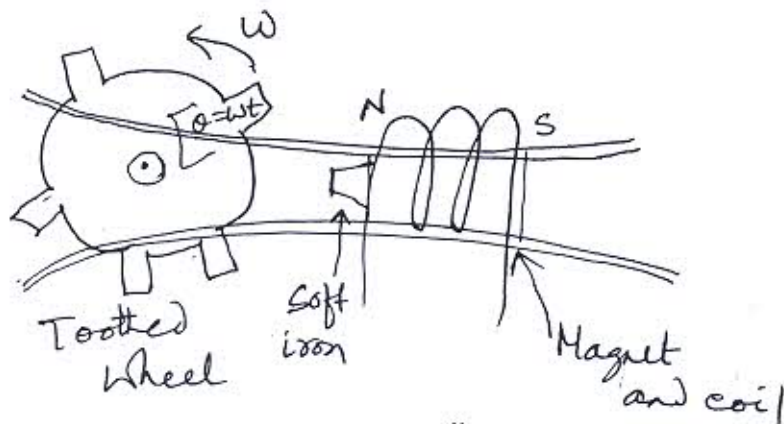
→ The induced emf in a conductor depends on the rate of change of flux linking with conductor.

$$E = - \frac{dN}{dt} \quad N \rightarrow \text{Total flux}$$

Construction:

→ It consists of a toothed wheel of ferro-magnetic material and a coil wound on a permanent magnet extended by a soft iron pole piece.

→ When the tooth is close to the pole piece reluctance is minimum but the reluctance increment with the tooth moves away from the pole piece.



→ Reluctance is maximum when the gap is adjustant to the pole piece and falls again as the next tooth approaches to pole piece.

The total flux linked by a core of 'n' turn coil is

$$N(\theta) = a + b \cos m\theta$$

Where, a = mean flux

b = amplitude

m = no. of teeth

$$E = -\frac{dN}{dt} = -\frac{dN}{d\theta} \times \frac{d\theta}{dt}$$

$$= bm \sin(m\theta) \frac{d\theta}{dt}$$

$$= bm \sin(m\theta) \omega_r$$

$$E = bm \omega_r \sin(m\alpha) \quad [\because \theta = \alpha]$$

$$\hat{E} = bm \omega_r \quad f = \frac{m\omega}{2\pi}$$